

Simple linear algorithm to estimate the space-time variability of precipitable water in the Araucanía Region, Chile

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Abstract

This work proposes a linear algorithm which relates precipitable water (PW) with altitude and distance from the coast, on a regional scale. For precipitable water, the ERA-Interim (ECMWF) database for the period 1989-2010 was used, while a digital elevation model was used for the geographical variables. The results obtained indicate statistical significance between the two variables ($p < 0.01$), with a confidence level of 99%. The model makes it possible to describe the mean monthly space-time variability of precipitable water, stratifying the study area into clearly differentiated zones.

Keywords: linear algorithm, precipitable water, digital elevation model.

1. Introduction

Atmospheric water vapour is the principal contributor to the greenhouse effect and plays a key role in our understanding of the Earth's climate. Precipitable water (PW) is the amount of vertically integrated water vapour and can be expressed in g cm^{-2} , or as the height of an equivalent column of liquid water in cm. Traditionally, there have been three atmospheric water vapour observing systems on a global scale: radio soundings, general circulation models and satellite observations. PW is an important component of the hydrological cycle and is adopted as an input variable in global climatological studies. Moreover, it has the potential to support hydrological, biospheric and atmospheric modelling efforts, on both local and regional scales, since it is widely used in energy budget and evapotranspiration studies (Hadjimitsis *et al.*, 2011). Furthermore, PW is an essential requirement in atmospheric correction of high spatial resolution satellite data, and it is also necessary for enhancing the precision of land surface temperature estimates obtained from satellite data (Wan, 1999; Morales *et al.*, 2002; Morales and Parra, 2002; Parra *et al.*, 2006; Vera *et al.*, 2010).

One way of obtaining the PW is through radio soundings or database compilations, such as those extracted from Moderate Resolution Imaging Spectroradiometer (MODIS) and ERA-Interim, an ensemble of meteorological data based on the Reanalysis carried out by the European Centre for Medium-Range Weather Forecasts. ERA-Interim (Dee *et al.*, 2011) considers information from 1 January 1989 to the

present, and can be accessed on line (<http://www.ecmwf.int/research/era/do/get/era-interim>). The information is presented in the form of both daily and monthly average values, and covers the whole planet with a grid resolution of 1.5 degrees of latitude and longitude. For each node of the grid, profiles are available for temperature, pressure, specific humidity and other variables.

The objective of the present communication is to propose a simple linear algorithm for estimating and describing the monthly mean space-time variability of precipitable water, on a regional scale, based on the geographical characteristics of the observation point.

2. Materials and methods

2.1 Study area

The study area is the Araucanía Region, Chile (Figure 1), with a total area of 31,840.3 km². The study area presents two well differentiated climatic characteristics. The northern part of the Region has a warm temperate climate with a short dry season (less than 4 months), while the part lying to the south of latitude -38° is associated with a wet temperate climate, with Mediterranean influence. The Region presents distinct geographical units: coastal plain, coastal mountain range, central depression, Andean pre-cordillera and Andes Mountains, with average altitudes varying between 200 and 2,000 m.a.s.l.

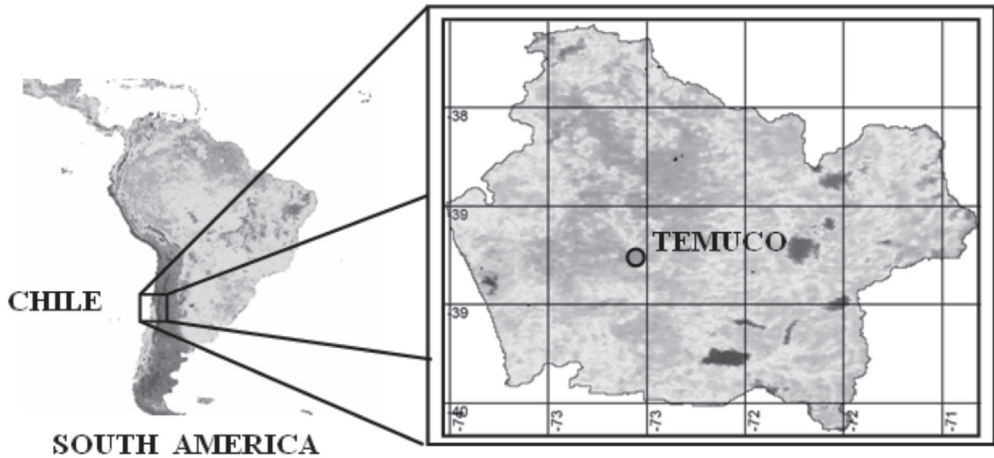


Figure 1. Study area: Araucanía Region, Chile.

2.2 Precipitable water

For this study, the average monthly precipitable water values were obtained from data supplied by ERA-Interim for the period 1989-2010. Considering that the grid resolution is around 166.5 x 166.5 km, the data were interpolated to bring them down to a resolution of 20 x 20 km, using kriging interpolation by blocks with a linear variogram. The interpolated information was used to apply downscaling (Fuentes *et al.*, 2000; Wetterhall *et al.*, 2007) to obtain the precipitable water vapour at a resolution of 1 km x 1 km, to coincide with the spatial resolution of one pixel of the NOAA satellite image. The following linear model is proposed for the parameterization of precipitable water as a function of geographical characteristics such as altitude and distance from the coast:

$$PW = A + B \cdot ALT + C \cdot DIL + \gamma \quad (1)$$

A, B and C are monthly mean coefficients depending on latitude and longitude; ALT is the altitude (m), DIL represents the distance from the coast (m) and

γ represents the error associated with estimation in g cm^{-2} . Equation 1 is founded because the amount of water vapour in the atmosphere is affected by temperature variations and depends on variations in altitude (ALT), and geographical conditions, such as distance to the Pacific Ocean (DIL) (AGU, 2002; Parwati *et al.*, 2007). The application of the model assumes the use of a digital elevation model, with ALT as a variable. In this study we used GTOPO30 (<http://edc.usgs.gov/products/elevation/gtopo30/gtopo30.html>), geo-referenced to the datum WGS84 (Figure 1).

3. Results

Table 1 shows, by month: regression coefficients A, B and C; the coefficient of determination (r^2); the statistical significance (p); and the standard error g . It may be seen that the proposal of the algorithm to describe the relation between precipitable water, altitude and distance from the coast is significant. In fact, the statistical significance, on average $p < 0.01$, indicates that the relation between the variables considered is statistically significant, with a confidence level of 99%.

The value of r^2 shows that the model used explains, on average, 83 % of the variability in precipitable water vapour, representing a strong relationship between the variables.

The time variability of coefficients A, B and C of equation (1) for the Araucanía Region of Chile are shown in Figure 2.

Table 1. Values of coefficients A and B for the regression. $PW = A + B \cdot ALT + C \cdot DIL + \gamma$. The statistical values of the coefficient of determination, r^2 , standard error g and statistical significance, p, are also indicated.

Month	A (g cm^{-2})	B $\times 10^{-5}$ ($\text{g cm}^{-2} \text{ m}^{-1}$)	C $\times 10^{-5}$ ($\text{g cm}^{-2} \text{ m}^{-1}$)	g $\times 10^{-2}$ (g cm^{-2})	r^2	p
January	1.53828	4.4402066	-0.187775	6.6467	0.84	0.0000
February	1.56530	5.0148432	-0.177534	7.0048	0.80	0.0000
March	1.57972	5.2872668	-0.197890	7.4967	0.81	0.0000
April	1.43329	4.9759926	-0.206196	7.3831	0.83	0.0000
May	1.38728	5.1646561	-0.209144	7.5440	0.83	0.0000
June	1.31359	4.6527804	-0.201236	7.3766	0.83	0.0000
July	1.16480	4.2493843	-0.183105	6.5428	0.84	0.0000
August	1.17262	4.1886861	-0.180572	6.3217	0.84	0.0000
September	1.12749	3.9161601	-0.161547	5.8278	0.83	0.0000
October	1.21776	3.7382387	-0.159670	5.7643	0.83	0.0000
November	1.34550	3.6931073	-0.167441	5.9018	0.84	0.0000
December	1.50005	3.9896655	-0.182630	6.3881	0.84	0.0000

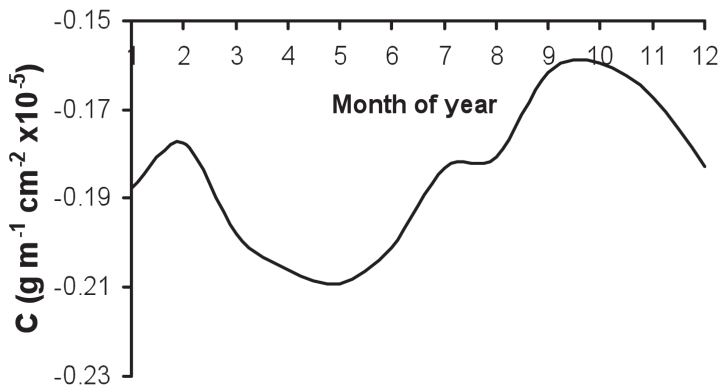


Figure 2. Time variability of coefficients A, B and C of regression $W = A + B \cdot ALT + C \cdot DIL + \gamma$ in the Araucanía Region, Chile.

In order to obtain categories with uniform values for PW, a non-hierarchical cluster analysis was done using the minimum distance criterion (Perez, 2004). This technique allowed pixels with similar precipitable water vapour values to be considered in a single cluster, while pixels with different values were located in other clusters. Figure 3 shows the result of the clus-

ter analysis carried out on the monthly mean values; it may be clearly observed that the precipitable water is stratified into different zones. These correspond to the coastal area, characterised by the Nahuelbuta coastal range; the central depression; the Andean pre-cordillera; and the Andes Mountains.

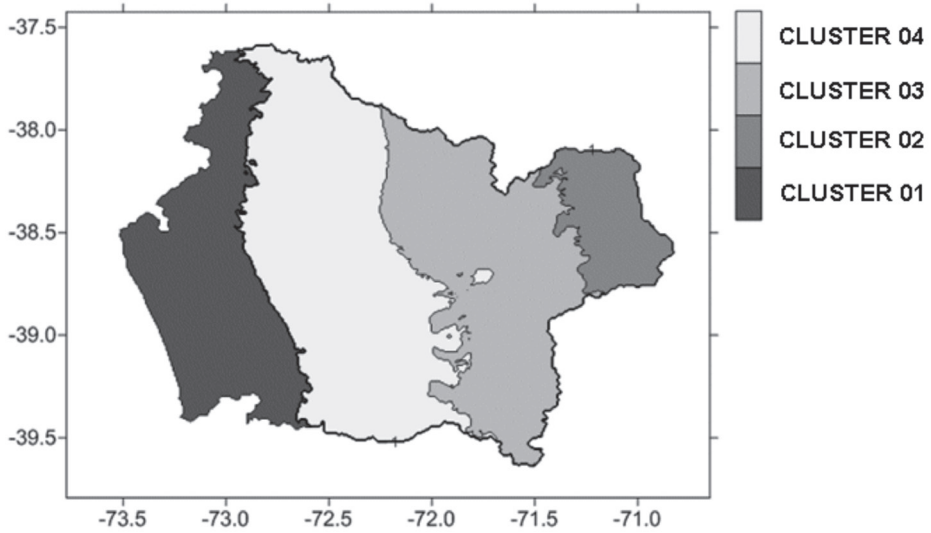


Figure 3. Cluster behaviour zones for precipitable water in the Araucanía Region, Chile.

The result of the cluster analysis in the study area shows that precipitable water vapour follows space-time trends defined at a mean monthly level, which are very similar to the Köppen climate classification system. This fact is based on the observed dependence on geographical position, altitude and, in the case of this study area, distance from the coast. The same descriptors are used to model the spatial distribution of the climate in the study area, with satisfactory results (Díaz *et al.*, 2010). In the study area, water vapour is transported primarily from the Pacific Ocean (Morales *et al.*, 2009).

Table 2 shows the statistics describing each cluster in monthly values, with columns for the average (AVG), the Range ($W_{\max} - W_{\min}$) (RAN), and the coefficient of variation in percentage (CV) of the precipitable water for each cluster in the time period considered.

Figure 4 shows the behaviour of the precipitable water for each cluster in the study area. In general terms, all the curves follow a similar comportment over time, with maximum values concentrated between January and March. This coincides with maximum solar radiation at median latitudes in the southern hemisphere, and therefore with a considerable increase in evaporation from the Pacific Ocean.

In addition, it can be seen that the cluster with the greatest precipitable water is cluster 1, the coastal zone, while the clusters with intermediate values are the central depression and the pre-cordillera. Cluster

2 equates to the zone with the lowest precipitable water content, corresponding to the Andes range in the Araucanía Region.

Table 2. Average monthly values (AVG), range (RAN) and coefficient of variation in percentage (CV) of PW for each cluster in the period 1989-2010.

Cluster	1			2			3			4		
	AVG	RAN	CV	AVG	RAN	CV	AVG	RAN	CV	AVG	RAN	CV
JAN	1.493	0.124	2.238	1.113	0.070	1.380	1.240	0.123	2.407	1.358	0.128	2.699
FEB	1.524	0.121	2.080	1.175	0.070	1.214	1.291	0.129	2.065	1.398	0.124	2.386
MAR	1.533	0.133	2.298	1.140	0.076	1.392	1.271	0.138	2.391	1.392	0.136	2.724
APR	1.384	0.136	2.655	0.967	0.077	1.734	1.107	0.134	2.957	1.236	0.139	3.220
MAY	1.338	0.139	2.772	0.917	0.079	1.846	1.057	0.138	3.121	1.187	0.141	3.399
JUN	1.265	0.134	2.833	0.856	0.076	1.936	0.993	0.133	3.254	1.120	0.139	3.499
JUL	1.121	0.122	2.915	0.749	0.069	2.014	0.873	0.121	3.367	0.989	0.126	3.609
AUG	1.129	0.120	2.861	0.762	0.068	1.938	0.885	0.119	3.274	0.999	0.124	3.514
SEP	1.089	0.107	2.651	0.763	0.061	1.727	0.872	0.105	2.934	0.973	0.109	3.209
OCT	1.179	0.106	2.412	0.855	0.060	1.532	0.964	0.105	2.649	1.065	0.109	2.905
NOV	1.305	0.112	2.293	0.962	0.064	1.456	1.077	0.113	2.524	1.184	0.120	2.770
DEC	1.456	0.122	2.247	1.081	0.070	1.423	1.206	0.124	2.449	1.324	0.132	2.708

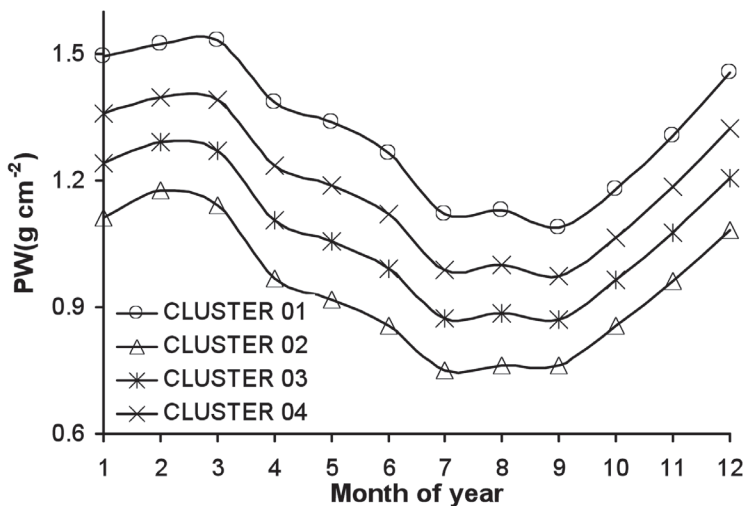


Figure 4. Variability over time in the monthly mean PW, period 1948-2005.

4. Conclusions

A linear algorithm relating precipitable water to altitude and distance from the coast makes it possible to estimate and describe the space-time variability of precipitable water. This study, done on a regional scale, produced a statistical significance between the two variables of $p < 0.01$, indicating that the relation is statistically significant, with confidence level 99%.

A non-hierarchical cluster analysis, applied to the values for precipitable water, allowed the Araucanía Region to be stratified into different uniform zones, with the highest values of W found in the coastal zone, intermediate values in the central depression and pre-cordillera, and the lowest in the Andes range.

The proposed model offers an operational solution for obtaining PW information as a monthly mean when no daily information from radio soundings or satellite platforms is available. This provides an entry variable on which to base atmospheric corrections to thermal images, e.g. those supplied by the NOAA and TERRA platforms. This allows for applications in agricultural sciences when there is a need to estimate particular biophysical variables, such as thermal inertia and evapotranspiration, which appear to be closely linked to soil surface temperature.

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