



Article

Effect of Substitutional Metallic Impurities on the Optical Absorption Properties of TiO₂

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Abstract: (TiO₂) is both a natural and artificial compound that is transparent under visible and near-infrared light. However, it could be prepared with other metals, substituting for Ti, thus changing its properties. In this article, we present density functional theory calculations for Ti_(1-x)A_xO₂, where A stands for any of the eight following neutral substitutional impurities, Fe, Ni, Co, Pd, Pt, Cu, Ag and Au, based on the rutile structure of pristine TiO₂. We use a fully unconstrained version of the density functional method with generalized gradient approximation plus the U exchange and correlation, as implemented in the QUANTUM ESPRESSO free distribution. Within the limitations of a finite-size cell approximation, we report the band structure, energy gaps and absorption spectrum for all these cases. Rather than stressing precise values, we report on two general features: the location of the impurity levels and the general trends of the optical properties in the eight different systems. Our results show that all these substitutional atoms lead to the presence of electronic levels within the pristine gap, and that all of them produce absorptions in the visible and near-infrared ranges of electromagnetic radiation. Such results make these systems interesting for the fabrication of solar cells. Considering the variety of results, Ni and Ag are apparently the most promising substitutional impurities with which to achieve better performance in capturing the solar radiation on the planet's surface.

Keywords: DFT calculations; optical absorption properties; electronic properties

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1. Introduction

Bulk phases and nanoparticles of titanium oxide (TiO₂) have received considerable scientific and technological interest, mainly because of the large number of applications in diverse fields. Cosmetics [1], photocatalysis [2], dye-sensitized solar cells [3] and gas sensing [4] are some examples of how these materials have captured researchers' interest. Even TiO₂ has been suggested for photovoltaic applications [5,6], despite its wide bandgap allowing electromagnetic absorption just beyond the ultraviolet range, which is practically absent in the solar radiation reaching the surface of the Earth. However, some substitutional impurity types (A) can increase the Ti_(1-x)A_xO₂ photoreactivity in the visible region, where the solar radiation reaches a maximum power. In fact, even some near-infrared bands could be considered in the development of multi-junction solar cells [7].

The electronic structure of doped TiO₂ has been studied in previous works [5,8], where the focus has been on the 3d transition metals acting as impurities (V, Cr, Mn, Fe, Co and Ni). For example, a first-principles study considered pristine TiO₂ in its rutile phase (which exhibits a rigid tetragonal structure with $a = 4.594$ and $c = 2.959$ Å as lattice vectors), while the doped system was in the form Ti₇A₁O₁₆, which corresponds to a (2 × 2 × 1) rigid

supercell [8]. The effects of single 3D transition metal impurity doping the TiO_2 matrix were studied based on F-LAPW [9] with GGA, as implemented in WIEN97 code [10]. Although the bandgap for pristine TiO_2 was found to be 1.9 eV (much smaller than the experimentally observed value of 3.1 eV [11,12]), the main conclusions were that 3D metal doping creates electronic levels in the pristine bandgap. Moreover, as the atomic number of the dopant increases, these localized levels shift to lower energy values.

Similarly, further first-principles calculations [5] showed that V, Cr, and Fe impurities narrow down the bandgap of pristine TiO_2 (starting from a calculated value of 2.3 eV for the bandgap), which was corroborated through UV-vis spectrometry, in this way verifying the significant role of ion implantation in the red-shift absorbance spectrum.

Impurities coming from the 3d and 4d series of transition metals were also incorporated in a matrix corresponding to the anatase phase of TiO_2 . The starting point was the calculated pristine bandgap that just reached 2.21 eV. However, the more important qualitative result was that most of the transition metals were able to narrow it down [13], which led to an improvement in the photoreactivity of TiO_2 in its different forms. When the on-site Coulomb interaction was incorporated through a GGA+U approach in the first-principles calculations of this system [14], the calculated bandgap agreed with the experimental value (3.21 eV).

The effect of the concentration of Fe impurities in the anatase phase has also been studied, showing that the bandgap of Fe-doped TiO_2 decreases as the Fe doping level increases. This is an indication of the important changes in TiO_2 's electronic properties due to the change in the orbitals following substitutional impurity.

Bandgaps for the rutile phase that are closer to the experimental values can be calculated by including on-site Coulomb corrections. For example, by including corrections between 3d orbital electrons of Ti atoms and the 2p O orbital electrons under the LDA+U formalism [15], it was possible to obtain a bandgap of 3.1 eV, which is quite close to the experimental value [11,12]. In this manner, it was also shown that correction parameters affect only the behavior of the conduction band, while values higher than 7 eV only allow for an unphysical description of the electronic interactions. The results are dramatically improved when correlation corrections are additionally introduced to the O 2p orbitals.

In this work, we will investigate the electronic, structural, and geometrical properties of TiO_2 bulk systems with neutral substitutional impurities. We will focus on the following impurity types: 3d transition metals (Fe, Co Ni) and noble metals (Cu, Ag, Au, Pd, Pt). Such a selection allows for a systematic study on the effect of element groups 10 and 11, while Fe and Co act as references for our calculations. In Section 2, we present the theoretical approach and computational details corresponding to the structural relaxation of the system, which includes on-site Coulomb corrections under the LDA+U formalism. Section 3 is devoted to the results (structural, density of states, and optical results) and their corresponding discussion. Finally, in Section 4 we summarize some conclusions.

2. Theoretical Approach and Computational Details

Our approach to this investigation was a two-step process beginning from the density functional theory (DFT) level. We first used the Spanish Initiative for Electronic Simulations with Thousands of Atoms (SIESTA) [16] code to perform pre-optimization of the structure, obtaining reliable lattice constants, regardless of the electronic states at this point. Then, we invoked the QUANTUM ESPRESSO v6.3 [17] package to perform definite structural relaxation (starting from the coordinates obtained with SIESTA), now including Hubbard's corrections to account for the bandgap in our pristine metallic matrix oxide.

For the pre-optimization, we used the free distribution computational package SIESTA v4.0 to carry out density functional theory (DFT) calculations following the generalized gradient approximation (GGA) proposed by Perdew–Burke–Ernzerhof (PBE) [18]. SIESTA makes use of numerical pseudo-atomic orbitals as basis sets to solve single-particle Kohn–Sham equations. In this way, the atomic cores are approximately described by nonlocal norm-conserving Troullier–Martins pseudopotentials [19] factorized in the Kleinman–

Bylander form [20]. The pseudo-potentials for O, Ti, Fe, Co, Ni, Cu, Pd, Ag, Pt and Au were obtained by considering the following valence configurations: $2s^2 2p^4$, $4s^2 3p^6 3d^2$, $4s^2 3d^6$, $4s^2 3d^7$, $4s^2 3d^8$, $4s^1 3d^{10}$, $5s^1 3d^9$, $5s^1 4d^{10}$, $6s^1 5d^9$, and $6s^1 5d^{10}$, respectively. Double- ζ doubly polarized basis sets were employed to describe the valence states. Further details on the pseudopotentials and basis sets used for the impurities, as well as on the pertinent tests, can be found in our previous works [21–23].

We performed structural relaxation under both a spin-polarized framework and a paramagnetic regime to address possible magnetic behavior. Additionally, we considered a $2 \times 2 \times 3$ unit cell of TiO_2 (see Figure 1a), which is equivalent to a Ti_mO_n super-cell ($m = 24$, $n = 48$). By imposing periodic boundary conditions, we mimicked pristine bulk TiO_2 , which can be modified by metallic substitutional impurities, leading to $\text{Ti}_{m-l}\text{A}_l\text{O}_n$, where A can be Fe, Co, Ni, Cu, Pd, Ag, Pt, or Au (see Figure 1b). In what follows, we focus on $l = 1$, which corresponds to an impurity concentration of $1/24 = 4.16\%$.

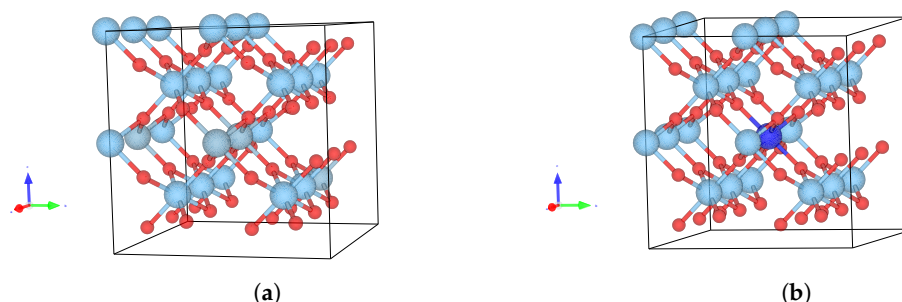


Figure 1. (a) $2 \times 2 \times 3$ unit cell modeling pristine TiO_2 in the rutile phase (Ti_mO_n) with $m = 24$ and $n = 48$. Ti (O) atoms appear represented in light blue (red). (b) A substitutional metallic impurity (blue ball) leading to $\text{Ti}_{m-l}\text{A}_l\text{O}_n$. In particular, $l = 1$ corresponds to an impurity concentration of 4.16%.

3. Results and Discussion

3.1. Structures and Energies

Table 1 summarizes the results for the relaxed structure, including the lattice constants a , b , c , c/a ratio, magnetic moment per unit cell, and energy difference per atom, depending on whether or not magnetic corrections were included. As can be observed, only slight variations were found in the lattice constants due to the presence of one impurity atom of any kind. This is not surprising since Table 1 contains values for the whole cell.

Table 1. Lattice constants, magnetic moment and $\Delta\epsilon_p$ for different substitutional metallic impurities on TiO_2 .

Impurity	a Å	b Å	c Å	c/a	Magnetic Moment μ_B/Cell	$\Delta\epsilon_p^{(a)}$ meV
Pristine	4.621	4.621	3.055	0.661	0.0	-
Fe	4.609	4.609	3.046	0.661	2.5	6.1
Co	4.602	4.647	3.046	0.662	1.0	1.0
Ni	4.603	4.602	3.046	0.662	0.0	-
Cu	4.605	4.605	3.058	0.664	2.0	−9.4
Pd	4.617	4.617	3.058	0.662	0.0	-
Ag	4.626	4.756	3.063	0.662	0.0	-
Pt	4.617	4.617	3.060	0.663	0.0	-
Au	4.628	4.627	3.065	0.662	0.3	0.0

^(a) $\Delta\epsilon_p = (E_p - E_s)/(l + m + n)$.

A host of differences were found for the magnetic moments per unit cell, ranging from 0 in several of them to 2.5 for iron.

Particularly notorious is the case of copper with $2.0 \mu_B/\text{cell}$. In general, magnetism does not play an important role in these systems, in which the magnetic moment for 4D and 5D metals is zero, just as in the case of the nickel system. Only in the case of iron do cobalt and copper show magnetism.

The magnetic moment per cell reported in Table 1 is of relative importance for Fe, Co and Cu only. This is a magnetic moment shared by the 72 atoms of the cell, so it has little weight in terms of the magnetic properties of the system.

Further calculations show that a paramagnetic configuration minimizes the total energy for the $\text{Ti}_{23}\text{CuO}_{48}$ and $\text{Ti}_{23}\text{AuO}_{48}$ systems. In fact, by defining the total energy difference per atom as $\Delta\epsilon_p = (E_p - E_s)/(l + m + n)$, where E_p and E_s correspond to the total energies in a paramagnetic and spin-polarized calculation, respectively, we can observe that thermal effects at room temperature (25 meV) are enough to demagnetize any of these systems (see the last column of Table 1). Even when the ferromagnetic behavior is observed experimentally for Cu-doped TiO_2 , the negligible remanent magnetization is in agreement with our results [24,25]. For these reasons, we concentrate on the calculation of properties based on the energy bands in the paramagnetic regime.

We also determined the formation energy for $\text{Ti}_{m-l}\text{A}_l\text{O}_n$, which is defined as follows [21,23,26–30]:

$$E_{\text{Formation}}[\text{Ti}_{m-l}\text{A}_l\text{O}_n] = E_{\text{Total}}[\text{Ti}_{m-l}\text{A}_l\text{O}_n] - E_{\text{Vac}}^*[\text{Ti}_{m-l}\text{O}_n] - lE_{\text{Atom}}[\text{A}]. \quad (1)$$

In this equation, A stands for the element acting as a substitutional impurity in pristine TiO_2 , $E_{\text{Total}}[\text{Ti}_{m-l}\text{A}_l\text{O}_n]$ corresponds to the total energy of the system, $E_{\text{Vac}}^*[\text{Ti}_{m-l}\text{O}_n]$ representing the total energy of the system presenting l vacancies of Ti, and $E_{\text{Atom}}[\text{A}]$ is the energy of an isolated atom of element A. In what follows, we have $m = 24$ and $n = 48$, and $l = 1$. Thus, for $\text{A} = \text{Ti}$, we can obtain the formation energy of pristine TiO_2 .

In a similar way, we found the binding energy, which is defined as follows:

$$E_{\text{Bind}}[\text{Ti}_{m-l}\text{A}_l\text{O}_n] = E_{\text{Total}}[\text{Ti}_{m-l}\text{A}_l\text{O}_n] - lE_{\text{Atom}}[\text{A}] - (m - l)E_{\text{Atom}}[\text{Ti}] - nE_{\text{Atom}}[\text{O}]. \quad (2)$$

Using Equation (2), we obtained the binding energy of pristine TiO_2 when $l = 0$ ($m = 24$ and $n = 48$), and thus we computed the delta binding energy per atom as follows:

$$\Delta E_{\text{Bind}} = \frac{E_{\text{Bind}}[\text{Ti}_{m-l}\text{A}_l\text{O}_n] - E_{\text{Bind}}[\text{Ti}_m\text{O}_n]}{l + m + n} \quad (3)$$

The formation energies and delta binding energies per atom for all the systems under study are shown in Figure 2a and 2b, respectively. These are presented as a function of the atomic number of the metallic impurity, while in the pristine case, they depicted by a horizontal dashed line. In both cases, we observe agreement with previously computed values for a $(\text{TiO}_2)_{10}$ cluster presenting substitutional impurities [23].

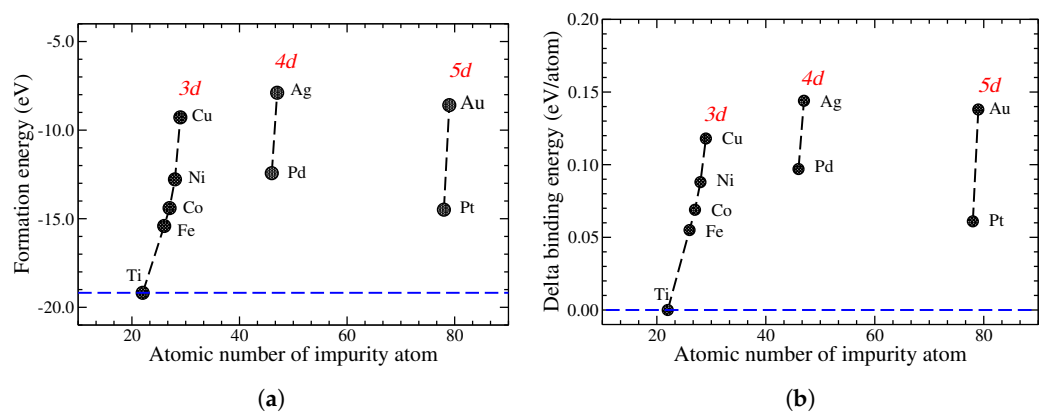


Figure 2. (a) Formation energy and (b) delta binding energy as a function of the atomic number of the metallic impurity in TiO_2 . The horizontal dashed line corresponds to pristine TiO_2 .

3.2. Electronic Density of States

Considering the low demagnetization energy barriers reported in Table 1, in what follows, we concentrate on the paramagnetic regime of each system. Of prime importance is the calculation of the Fermi level (E_{Fermi}), which will be used as the reference energy in the forthcoming diagrams. The calculated DOS curve is integrated up to the point when the number of electrons obtained coincides with the total number of electrons in the cell. The maximum energy reached in the integration process corresponds to E_{Fermi} .

The density of states (DOS) for different impurities, A, in $Ti_{23}AO_{48}$ is presented in different colors in Figures 3–5. The total DOS for pristine TiO_2 is depicted in the gray curve. The vertical red dashed lines indicate the Fermi level (left) and the first unoccupied state (right) in each case, and they are mere visual guide with which to identify the bandgap. We now discuss these figures collectively.

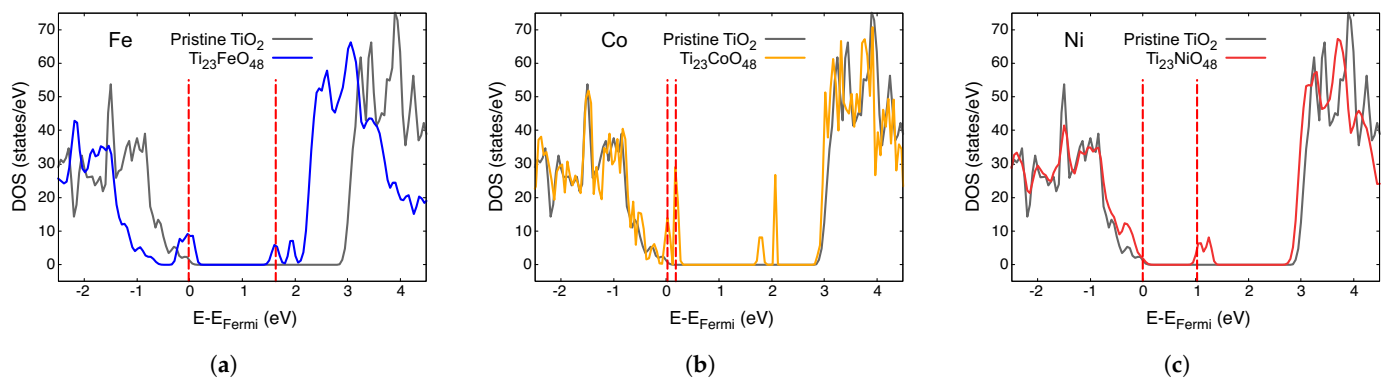


Figure 3. Density of states of paramagnetic $Ti_{23}AO_{48}$: (a) A = Fe; (b) A = Co and (c) A = Ni. The DOS for pristine TiO_2 is plotted gray in each case. The vertical red dashed lines are visual guides with which to identify the bandgap.

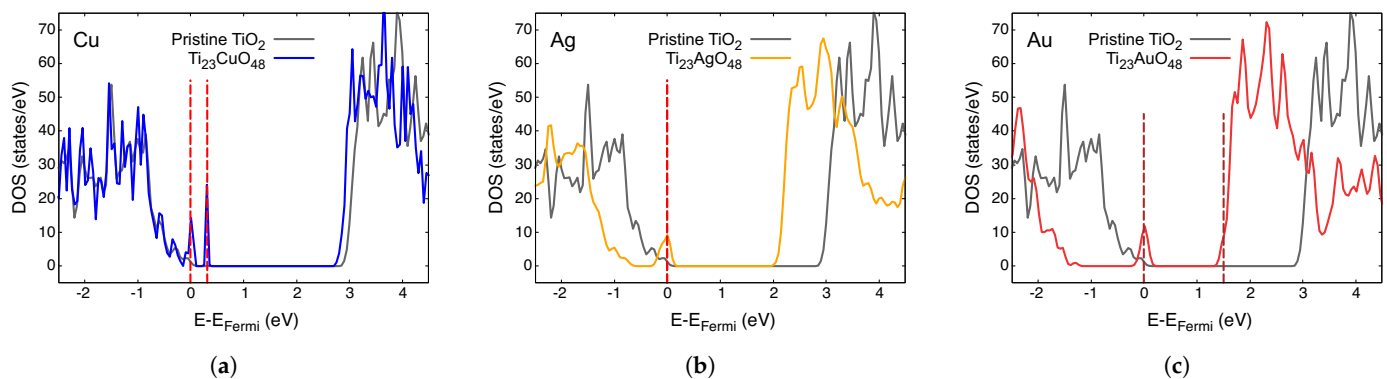


Figure 4. Density of states of paramagnetic $Ti_{23}AO_{48}$: (a) A = Cu; (b) A = Ag; and (c) A = Au. The DOS for pristine TiO_2 is plotted in gray in each case. Vertical red dashed lines are visual guides with which to identify the bandgap.

The first general observation is that new, mostly narrow levels appear in the gap in all these cases, which indicates an effective decrease in the bandgap compared with that of pristine crystal. The case of Ni is probably the simplest to analyze; consider Figure 3c, showing the Fermi level just at the top of the lower band. Impurity-empty levels appear around 1 eV above E_{Fermi} , which is a clear indication of the lower energy absorption possibilities, as we will discuss in the next section.

For all the other metals in the preceding figures, E_{Fermi} lies on an impurity band or just under it. The presence of empty levels just over E_{Fermi} creates new dynamics for these systems, which is important for their optical properties.

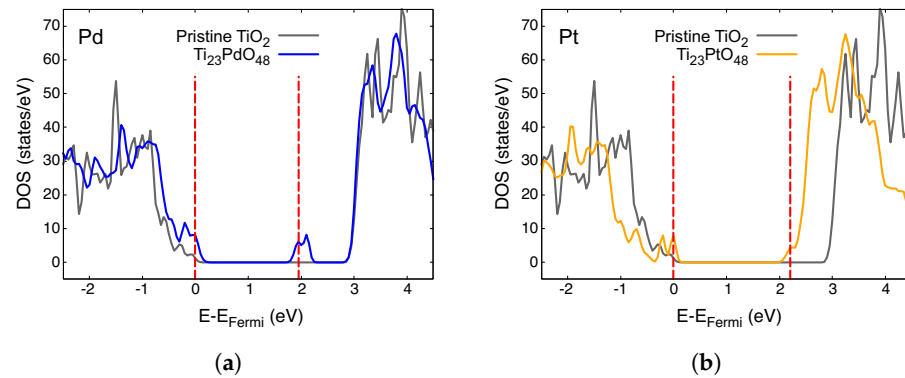


Figure 5. Density of states of paramagnetic Ti₂₃AO₄₈: (a) A = Pd; (b) A = Pt. The DOS for pristine TiO₂ is plotted in gray in each case. The vertical red dashed lines are visual guides with which to identify the band gap.

3.3. Optical Absorption Properties

The electromagnetic absorption spectrum is obtained by applying linear optical response approximation. In this way, the imaginary part of the dielectric function, $\epsilon_i(\omega)$, is related to the optical absorption coefficient, $\kappa(\omega)$, through the following equation:

$$\kappa(\omega) = \frac{\omega \epsilon_i(\omega)}{c n(\omega)}, \quad (4)$$

where $\hbar\omega$ corresponds to the incident photon energy, n is the refractive index of the pristine material, and c is the speed of light. The *epsilon.x* toolset, a post-processing code available in the QUANTUM ESPRESSO [17] v6.3 package, is employed to obtain the complex dielectric function. Thus, in the framework of band theory without electron hole interaction, $\epsilon_i(\omega)$ can be obtained using Drude–Lorentz equations [31–33]. Such approximation is enough to obtain general trends of the optical properties of the doped system, so we estimate more sophisticated treatments using the GW Bethe–Salpeter equation [34].

Figure 6 shows the imaginary part of the dielectric function, ϵ_i , obtained for the paramagnetic regime of Ti₂₃AO₄₈: A = Fe, Co, Ni (Figure 6a); A = Cu, Ag, Au (Figure 6b). Any one of these substitutional impurities improves the electromagnetic absorption of pristine TiO₂ (whose ϵ_i is depicted in gray). This is especially relevant for the visible spectrum (between two vertical lines) and the adjacent near-infrared transition because of their possible applications in photovoltaic technologies.

The Fermi level of the Ti₂₃FeO₄₈ system lies at the center of a narrow impurity band, thus allowing absorptions from the valence band (VB) approximately below 1.5 eV (Figure 3a). Absorptions of a higher energy (with that of a broad structure at around 1.6 eV in Figure 6) receives contributions originating from lower valence states and also from those ending in impurity levels under 2 eV at the top of Figure 3.

The imaginary part of the dielectric function for Ti₂₃CoO₄₈ (also in Figure 6a) shows that the first band more is abundant and displaced to lower energies, which is due to the several impurity levels just over E_{Fermi} and the proximity of states in VB.

The spectrum of Ti₂₃NiO₄₈ in Figure 6a presents two leading structures at about 1.1 eV and 1.8 eV. The former is sustained via transitions from the edge of the VB to the impurity doublet level at 1 eV. Next, we find a broader and more pronounced structure centered at 1.8 eV corresponding to transitions from more abundant, deeper states at the VB. In fact, these last transitions are very desirable for solar cell applications.

The imaginary parts of the dielectric functions for the Ti₂₃CuO₄₈, Ti₂₃AgO₄₈ and Ti₂₃AuO₄₈ systems are presented in Figure 6b. Cu presents near-infrared absorptions because of impurity levels both below and above E_{Fermi} . The case of Ti₂₃AuO₄₈ presents a similar level of activity for the visible range due to transitions from the edge of the VB

to this impurity level, which leads to a weak imaginary part of the dielectric function at low or intermediate energies (Figure 6b). The case of $\text{Ti}_{23}\text{AgO}_{48}$ is like that with a Au impurity, with a very important difference: the edge of the VB is nearer the impurity level in the pristine gap, which leads to important optical activity in the red and infrared zone of the spectrum.

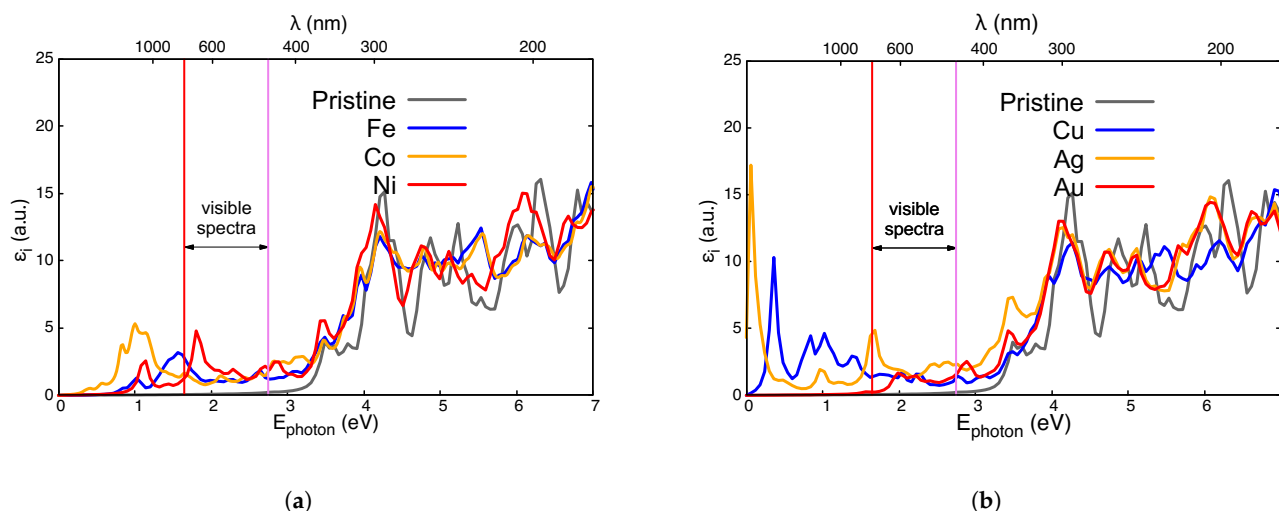


Figure 6. Imaginary part of the dielectric functions, $\epsilon_i(\omega)$, for $\text{Ti}_{23}\text{AO}_{48}$ compared with those for pristine TiO_2 (gray line). (a) A = Fe (blue line); A = Co (yellow line); and A = Ni (red line). (b) A = Cu (blue line); A = Ag (yellow line); A = Au (red line). Red and violet vertical lines are included to highlight the visible spectra.

Optical results for Pd and Pt are presented in Figure 7, which was created using the same techniques as those used for the previous figure. It can be observed that changes in the pristine case are not as important as those in previous cases, probably due to the lower hybridization of these 4D and 5D electrons in these wider atoms. Therefore, no activity in the infrared zone is to be found in any of these two systems. The presence of an impurity doublet just under 2 eV in Figure 5a explains the structure within the visible spectrum in Figure 7 for Pd (4D atomic configuration). No such impurity level is seen for Pt in Figure 5b, meaning that there is a weaker and blue-shifted absorption spectrum for Pt (5D atomic configuration in Figure 7).

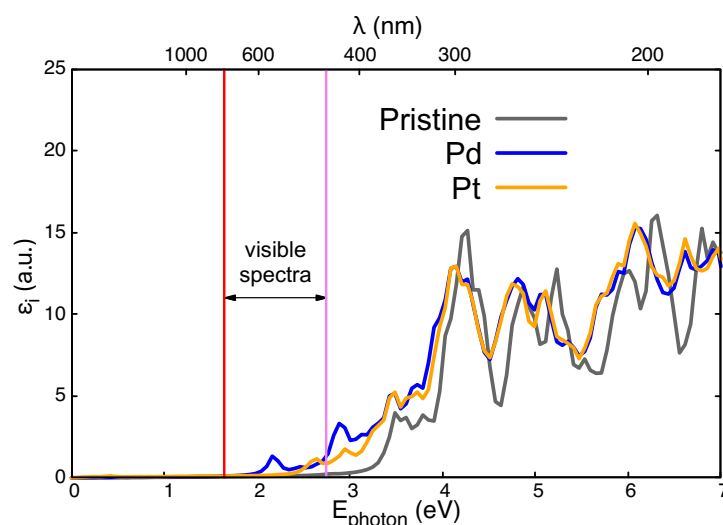


Figure 7. Imaginary part of the dielectric functions, $\epsilon_i(\omega)$, for $\text{Ti}_{23}\text{AO}_{48}$ compared with pristine TiO_2 (gray line). The cases of A = Pd and A = Pt are depicted by the blue and yellow lines, respectively. Red and violet vertical lines are included to highlight the visible spectra.

Since the impurities could have had different charge states [35], we obtained the absorption spectrum for charged impurities in the case of Ni and Ag, both of which exhibit absorption peaks in the visible spectrum. As shown in Appendix A, positively charged impurities shift the absorption peaks to higher energies, although they remain within the visible spectrum. However, particularly for Ni, negatively charged impurities degrade the optical absorption properties. Thus, it is necessary to extend the present study to include the different charge states of the impurities [36].

4. Conclusions

The first general conclusion is that the substitution of Ti by neutral metal elements in TiO₂ introduces electronic levels within the pristine energy gap. The density of states is different for each impurity, which provides several different channels for the possible applications.

The new energy gap can be very low (Cu, Ag, Co) or relatively wide (Pd, Pt). Intermediate energy gaps are obtained for Fe, Ni and Au. Such results are a consequence of the change in the overlap between the *d* states of the impurity with the 2*p* states of oxygen. Then, the introduction of energy levels within the pristine compound gap is possible, bringing in new electronic states that can enhance photocatalytic activity.

Quite relevant is the absorption activity in the visible and near-infrared spectrum, which can improve the performance of these materials such that they become good solar energy absorbents at room temperature. Therefore, Ni, Ag, Fe, Cu, and, to a lower extent, Au are good candidates for the visible or near-infrared absorption spectrum, as shown in Figure 6.

The optical absorption peaks of different impurities indicate the potential of their applications in multi-junction solar cells, which involve the stacking of materials with different bandgaps to absorb different frequencies of the visible spectrum, showing intense photo-response behavior.

In any case, our results reflect tendencies rather than exact values, so larger simulations with different concentrations (and large computer facilities) are needed to obtain more precise results. On the other hand, the different charge states of impurities must also be taken into account, which can be analyzed in future theoretical work. Having declared the limitations, we suggest Ni as the best candidate with which to substitute Ti in TiO₂ to test this proposal in real experiments.

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Abbreviations

The following abbreviations are used in this manuscript:

DFT	Density Functional Theory
DOS	Density of States
GGA	General Gradient Approximation
LDA	Local Density Approximation
NC-PP	Norm-conserving pseudo-potentials
VB	Valence band

Appendix A. Effect of Charged Impurities

Figure A1a,b show the absorption spectrum for charged Ni and Ag, respectively. The absorption peaks shifts to higher energies for positively charged impurities (Ni^+ , and Ag^+), but they remain within the visible spectrum. For negatively charged impurities, the Ag absorption peak diminishes but stays at the same energy. However, for Ni^- the absorption peak in the visible spectrum disappears.

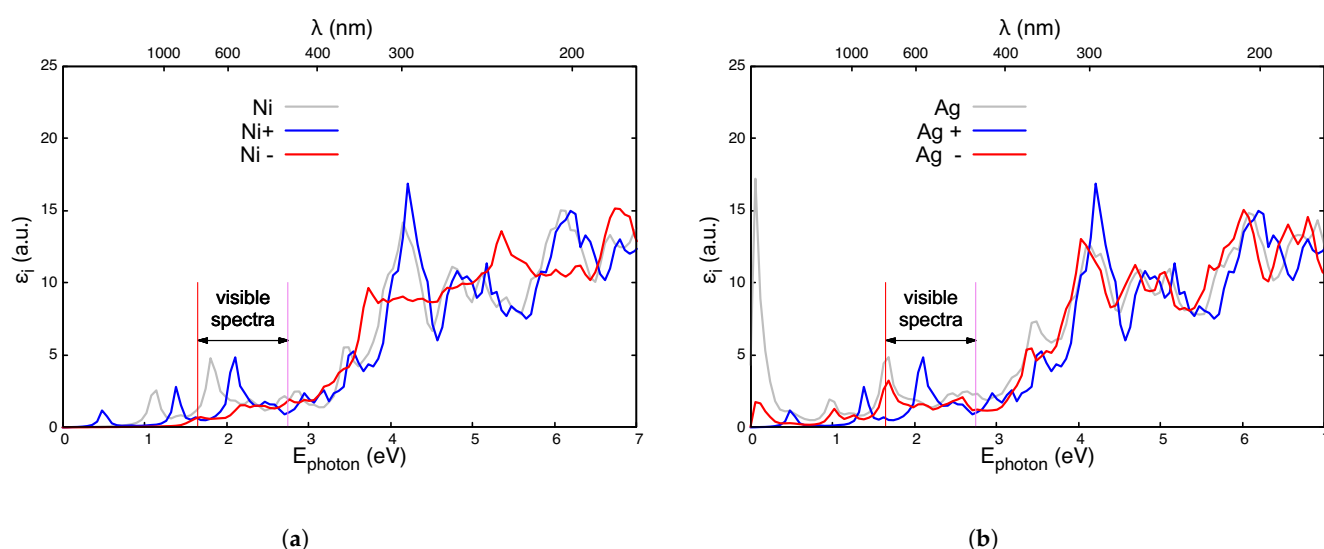


Figure A1. Imaginary part of the dielectric functions $\epsilon_i(\omega)$ for charged $\text{Ti}_{23}\text{AO}_{48}$ ($A = \text{Ni}, \text{Ag}$). (a) Neutral Ni (gray line), Ni^+ (blue line), and Ni^- (red line). (b) Neutral Ag (gray line), Ag^+ (blue line), and Ag^- (red line). Red and violet vertical lines are included to highlight the visible spectra.

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